

## COST-G gravity field models: application in SLR orbit determination

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**22<sup>nd</sup> International Workshop on Laser Ranging**  
**November 7-11, 2022, Yebes, Spain**

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# Combination Service for Time-variable Gravity Fields (COST-G)



22<sup>nd</sup> International Workshop on Laser Ranging  
November 7-11, 2022, Yebes, Spain

# International Association of Geodesy (IAG)

Int. Gravity  
Field Service



Int. Earth  
Rotation  
Service



Int. Gravimetric  
Bureau



Int. Geoid Service



Permanent  
Service for  
Mean Sea Level



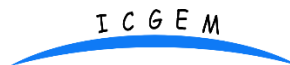
IGS INTERNATIONAL  
GNSS SERVICE



Int. Geodynamics and  
Earth Tide Service



Int. Laser  
Ranging  
Service



Int. Center for Global  
Earth Models



Combination Service for Time-variable Gravity Fields

Product Center of the IGFS



Int. VLBI  
Service



Int. DEM Service



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# International Gravity Field Service (IGFS)

## Gravity and geoid metadata

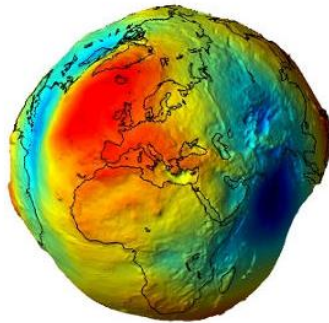
Online applications for the creation of metadata for gravity and geoid data. Service for searching the metadata database.

**g- $\mu$ eta**  
*the gravity metadata editor*  
*(v0.2.6 - beta edition)*

**N- $\mu$ eta**  
*the geoid metadata editor*  
*(v0.1.3 - alpha edition)*

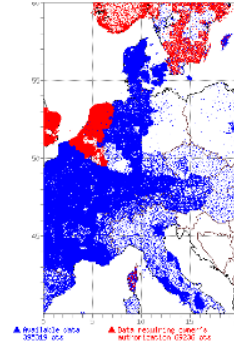
## Global Earth Models

Collection and archive of all existing global gravity field models, web interface for access to GEMs, model visualization and service.



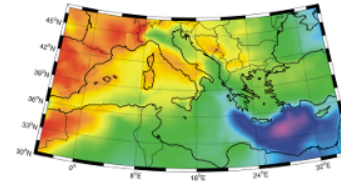
## Gravity data

Land, marine, airborne gravity data as point and gridded values. Absolute and relative gravity data, WGM



## Geoid

Geoid models and geoid determination software, geoid modeling processing methodologies



## SG and Earth tide data

Temporal variations of the Earth gravity field through long-term records from ground gravimeters, SG data, Earth tide data.



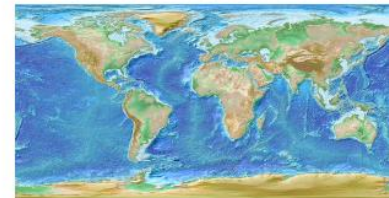
## Time-variable GEMs

Combined gravity field solutions in SH coefficients and spatial grids for hydrological, oceanic and polar ice sheets applications.



## DEM data

Digital Elevation Models, relevant software for DEM creation, assessment, manipulation and display, global relief and crustal models and spherical harmonic data sets.

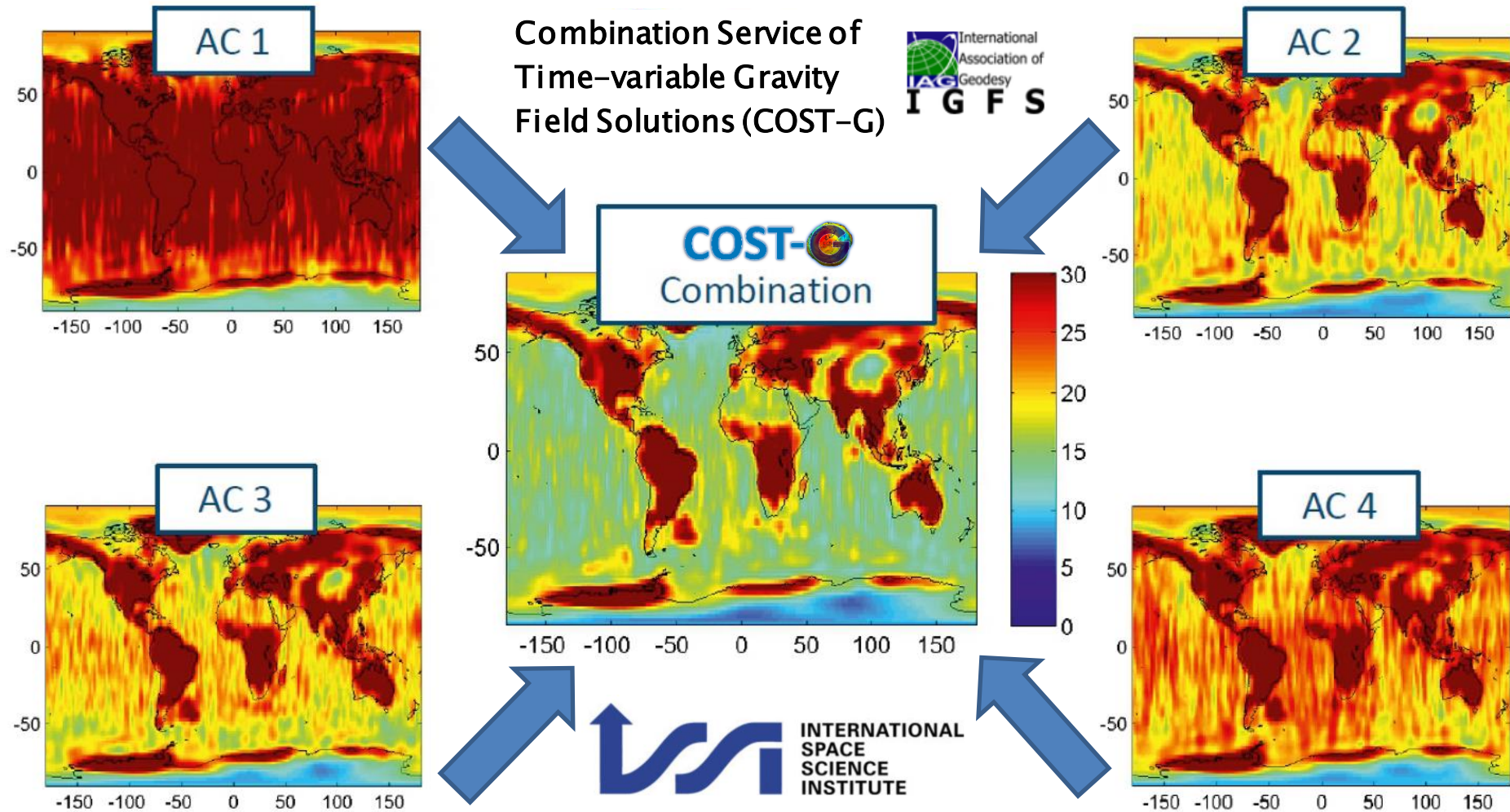


**COST-G is a product center of the**



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# Introduction to COST-G

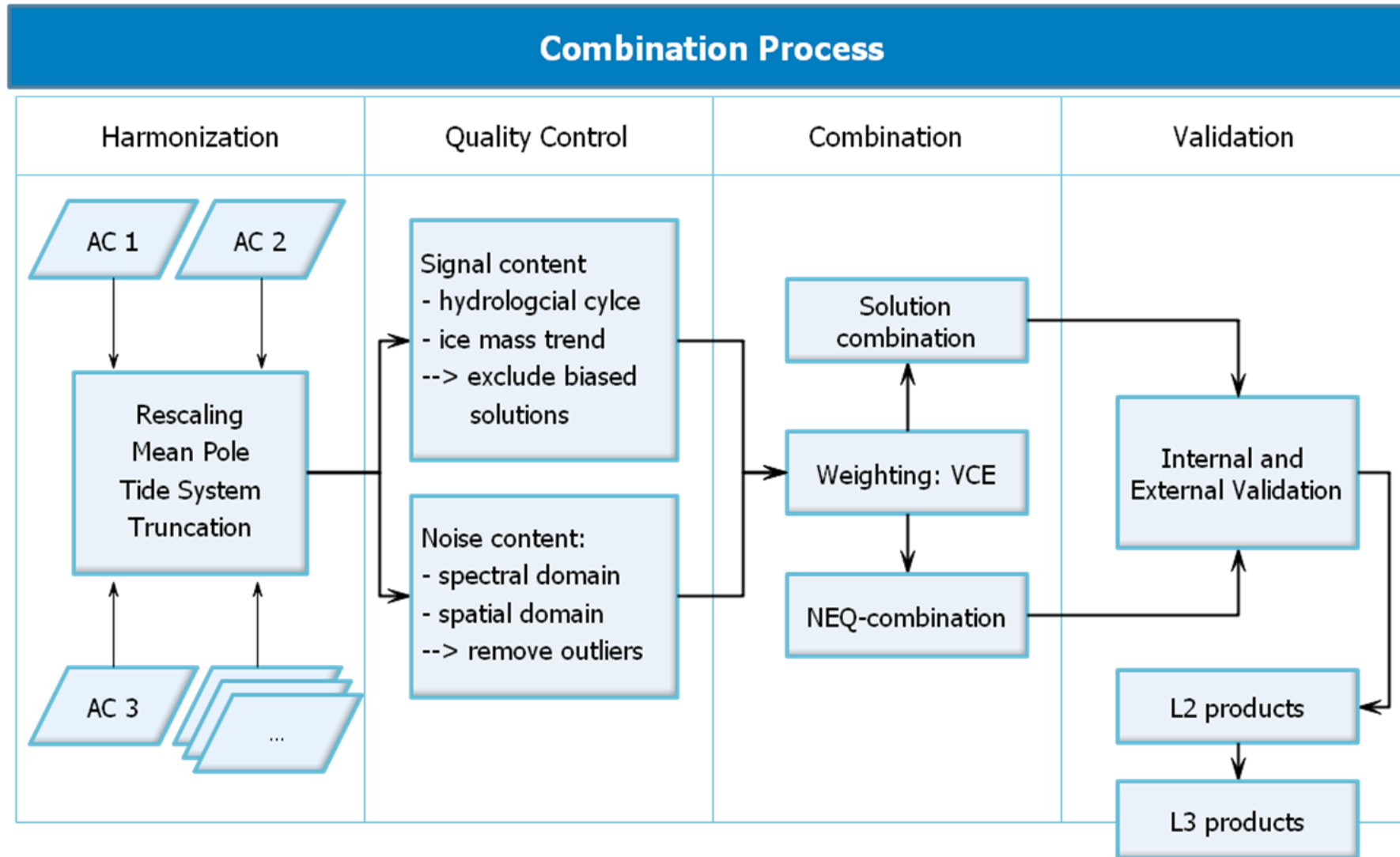


Improved and consolidated product integrating the strengths of all ACs

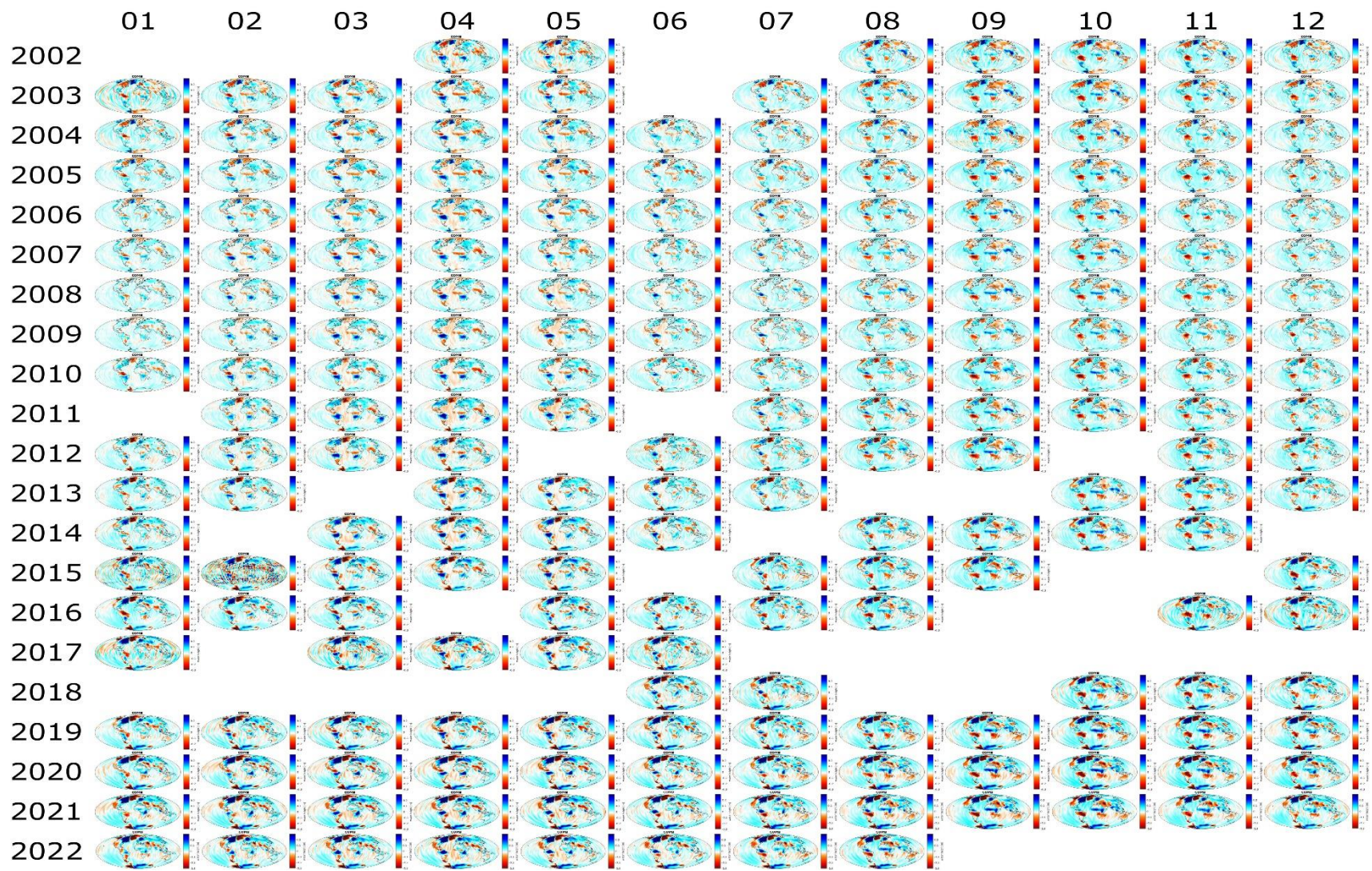


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# Workflow of COST-G



# GRACE-FO operational combined monthly gravity fields

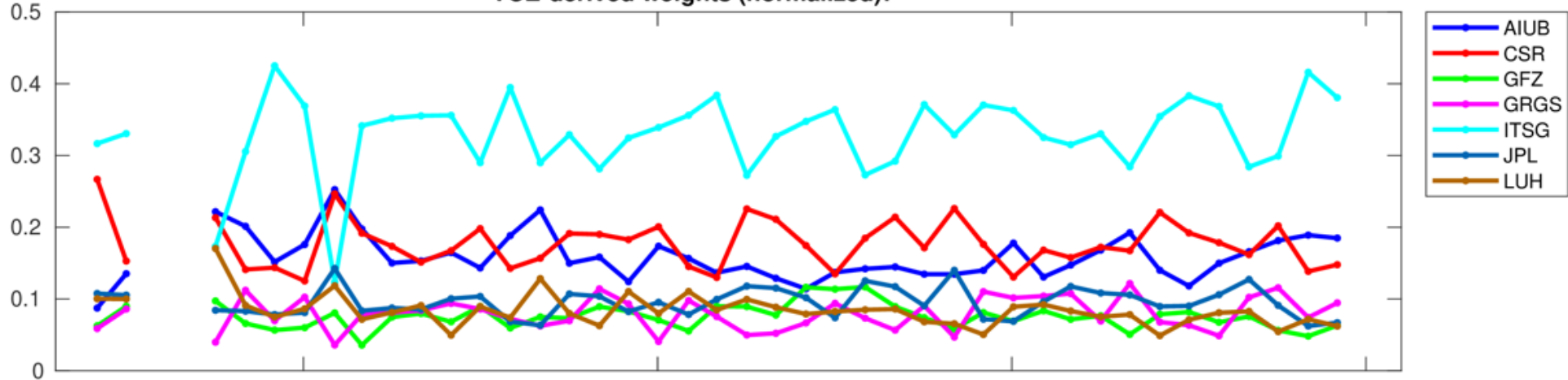


**Flawless and uninterrupted operational combination with a latency < 2-3 months.**

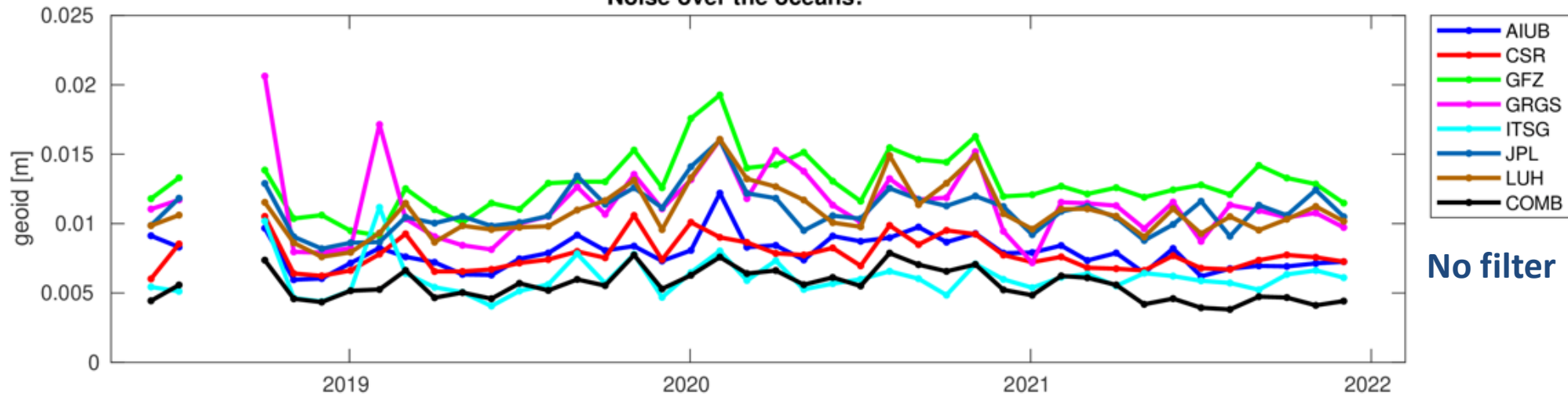


# Weighted combination and validation of the combined product

VCE-derived weights (normalized):



Noise over the oceans:

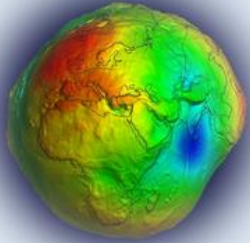


**Combination  
outperforms  
all individual  
solutions in  
2021**

**No filter**



# Where to get the products: <http://icgem.gfz-potsdam.de/series>



# ICGEM



## Gravity Field Solutions for dedicated Time Periods

The following gravity field time series are presently available:

GRACE and Grace-FO solutions from the Science Data System centers CSR, GFZ and JPL				collapse all
<b>- CSR</b>				<b>Center for Space Research at University of Texas, Austin</b>
CSR Release 05		monthly	UTCSR Level-2 Processing Standards Document, Rev 4.0 May 29, 2012	
CSR Release 06	DOI	monthly	UTCSR Level-2 Processing Standards Document, Rev 5.0 April 18, 2018	
CSR Release 06 (GFO)	DOI	monthly	UTCSR Level-2 Processing Standards Document, V 1.1 June 6, 2019	
<b>- GFZ</b>				<b>Helmholtz Centre Potsdam German Research Centre for Geosciences</b>
GFZ Release 05		monthly	weekly	GFZ GRACE Level-2 Processing, Revised Edition, January 2013
GFZ Release 06	DOI	monthly		GFZ GRACE Level-2 Processing Standards Document for Level-2 Products, Rev. 1.0, October 26, 2018
GFZ Release 06 (GFO)	DOI	monthly		GFZ GRACE Level-2 Processing Standards Document for Level-2 Products, Rev. 1.0, June 3, 2019
<b>- JPL</b>				<b>Jet Propulsion Laboratory</b>
JPL Release 05		monthly		JPL Level-2 Processing Standards Document, Release 05.1 November 3, 2014
JPL Release 06	DOI	monthly		JPL Level-2 Processing Standards Document, Release 06.0 June 1, 2018
JPL Release 06 (GFO)	DOI	monthly		JPL Level-2 Processing Standards Document, v 1.0 May 28, 2019

The processing standards to generate the GRACE Level-2 products of CSR, GFZ and JPL are also available in the Document Section of the GRACE archives at [GFZ ISDC](#) or [JPL PO.DAAC](#)

COST-G (International Combination Service for Time-variable Gravity Field)				collapse all
DSM		quarterly		Deterministic Signal Model
Grace	DOI	monthly		
Grace-FO	DOI	monthly		
Swarm	DOI	monthly		

[icgem@gfz-potsdam.de](mailto:icgem@gfz-potsdam.de)

For operational LEO-POD a fitted signal model is generated additionally to the monthly products.

The COST-G fitted signal model is available in the ICGEM.2-format from the International Center for Global Earth Models.

It is updated quarterly with the newest combined monthly GRACE-FO gravity fields.



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# COST-G FSM in ICGEM2.0-Format

CMMNT COST-G GRACE-FO deterministic gravity field model.

```
begin_of_head
format          icgem2.0
product_type    gravity_field
modelname       GSM-2_MODEL_GRFO_COSTG_test_2015
earth_gravity_constant 0.3986004415E+15
radius          0.6378136300E+07
max_degree     90
errors          formal
norm            fully_normalized
tide_system     tide_free
```

```
key   L   M   C           S           sigma C   sigma S   yyyyymmdd.xxxx  yyyyymmdd.xxxx  y
```

end\_of\_head

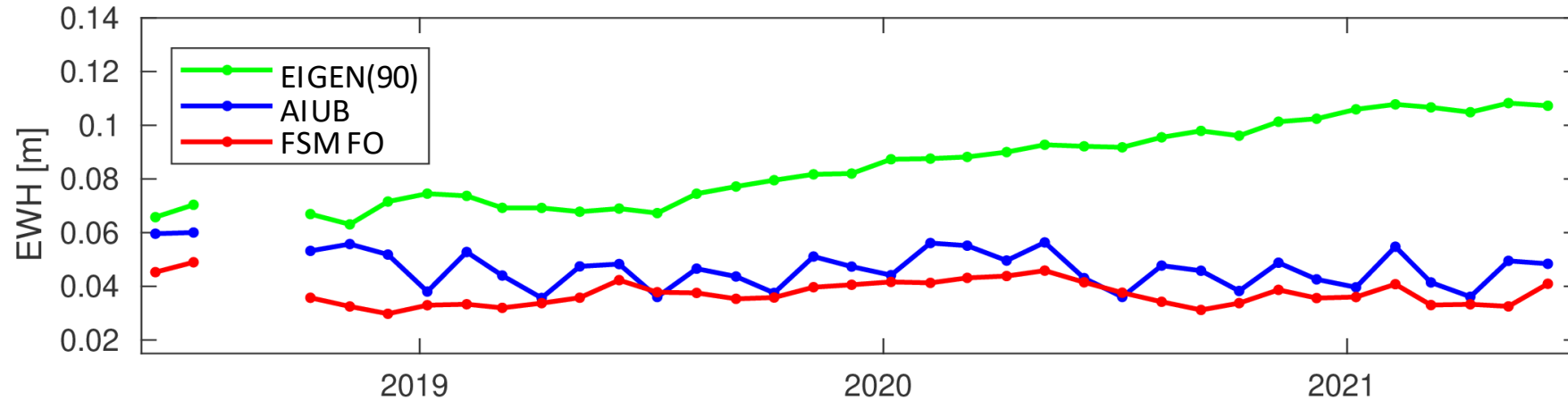
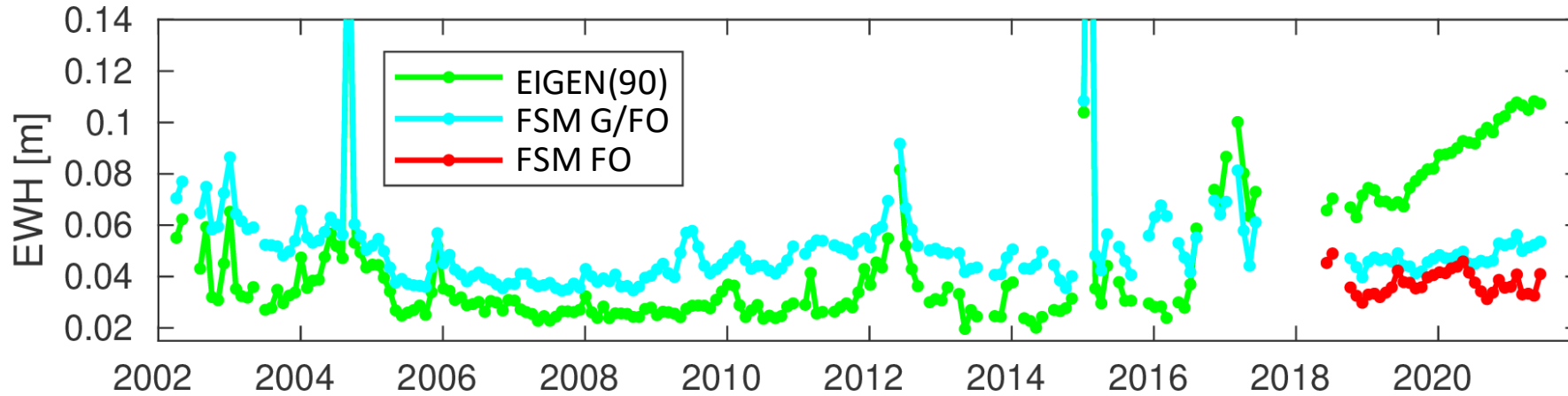
key	L	M	C	S	sigma C	sigma S	yyyyymmdd.xxxx	yyyyymmdd.xxxx	y
gfc	0	0	1.000000000000E+00	0.000000000000E+00	0.0000E+00	0.0000E+00			
gfc	1	0	0.000000000000E+00	0.000000000000E+00	0.0000E+00	0.0000E+00			
gfc	1	1	0.000000000000E+00	0.000000000000E+00	0.0000E+00	0.0000E+00			
gfct	2	0	-4.84165346490E-04	+0.000000000000E+00	6.0725E-11	0.0000E+00	20150101.0000	20180101.0000	
trnd	2	0	-7.39420829887E-11	+0.000000000000E+00	6.0842E-11	0.0000E+00	20150101.0000	20180101.0000	
acos	2	0	+4.13443094398E-11	+0.000000000000E+00	5.9933E-11	0.0000E+00	20150101.0000	20180101.0000	1.0
asin	2	0	+2.53863222596E-11	+0.000000000000E+00	6.6495E-11	0.0000E+00	20150101.0000	20180101.0000	1.0
acos	2	0	+2.65048085336E-11	+0.000000000000E+00	6.0809E-11	0.0000E+00	20150101.0000	20180101.0000	0.5
asin	2	0	-2.15182898423E-12	+0.000000000000E+00	6.4827E-11	0.0000E+00	20150101.0000	20180101.0000	0.5
...									



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# Fitted Signal Model (FSM) for operational LEO-POD

# RMS of differences (over land, 300 km Gauss): FSM - monthly gravity fields

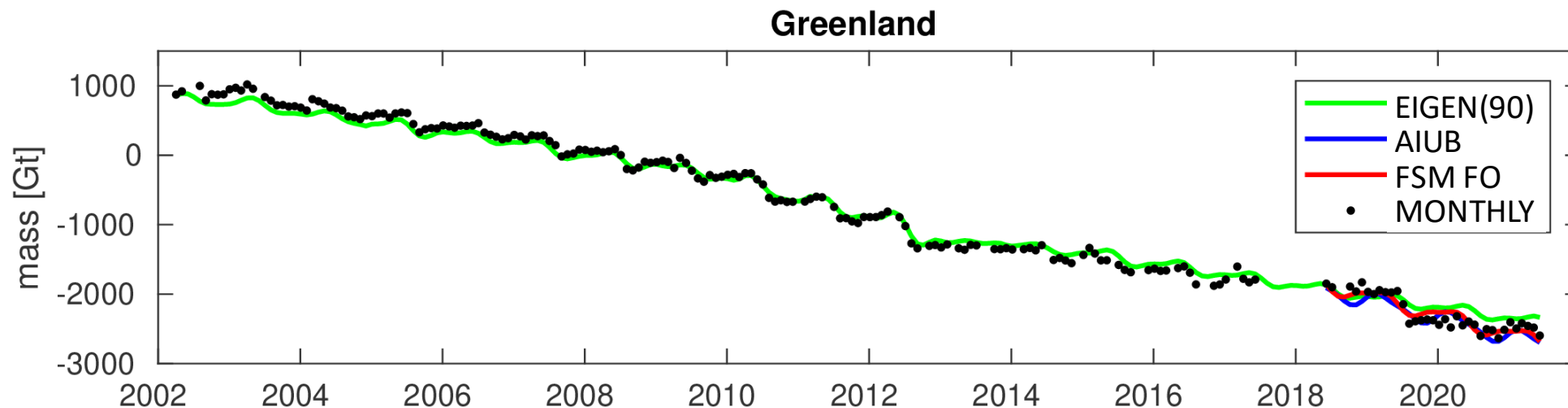


Operational precise orbit determination (POD) of low Earth orbiters (LEO) relies on a Earth gravity model including time-variable gravity (TVG).

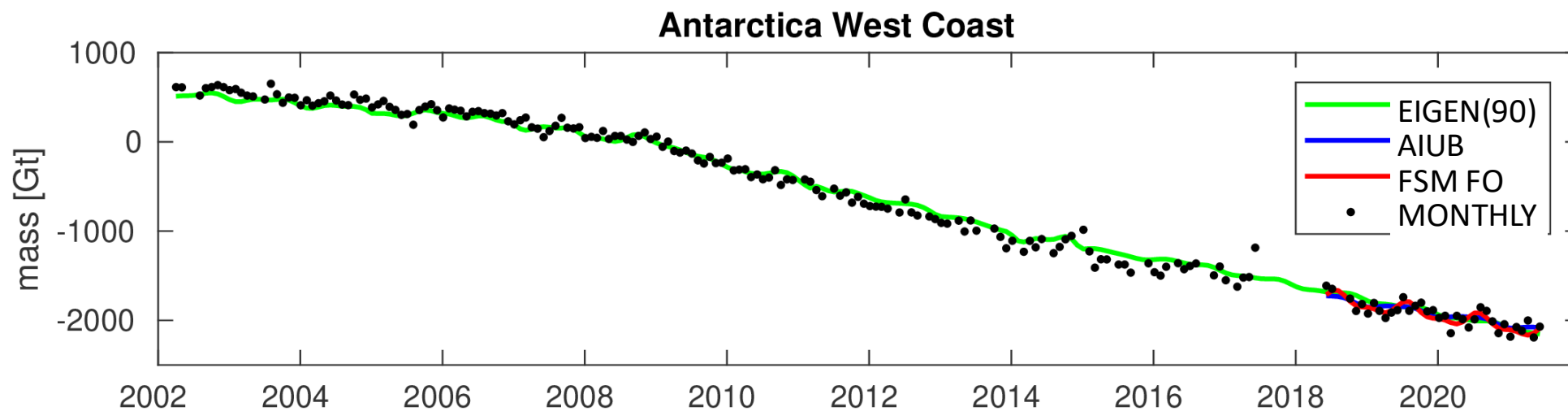
The EIGEN-GRGS-RL04 model (green) has been the standard for LEO-POD of altimeter satellites, but the extrapolation to the GRACE-FO period reveals large prediction errors.

For comparison, a model fitted to COST-G GRACE-FO gravity fields is shown (red).

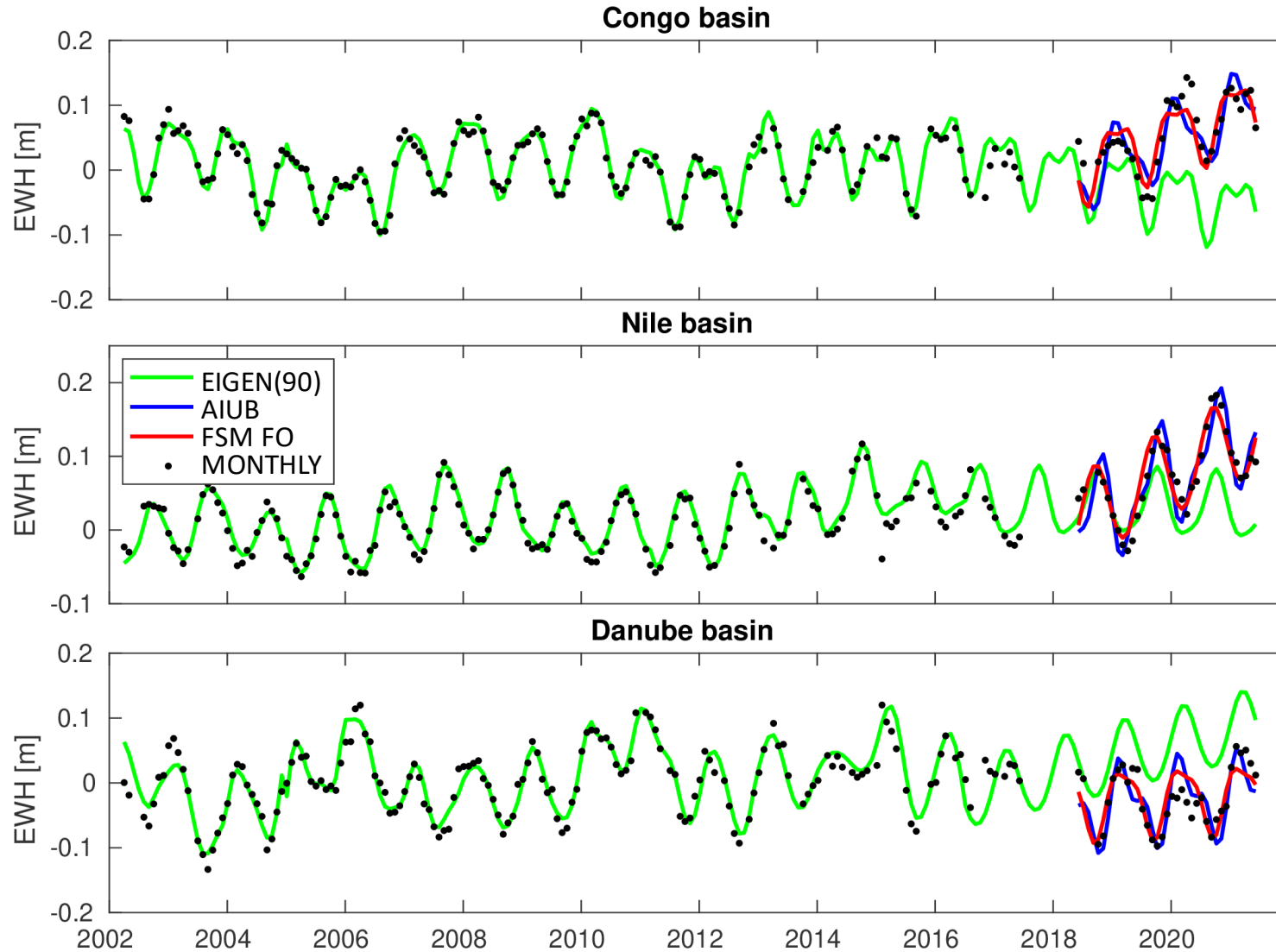
# Polar mass trend (no filter)



Surprisingly, the reason for the prediction error in the EIGEN-GRGS-RL04 model (green) seems not to be in regions with strong mass trends.



# Hydrological cycle in large river basins (300 km Gauss)



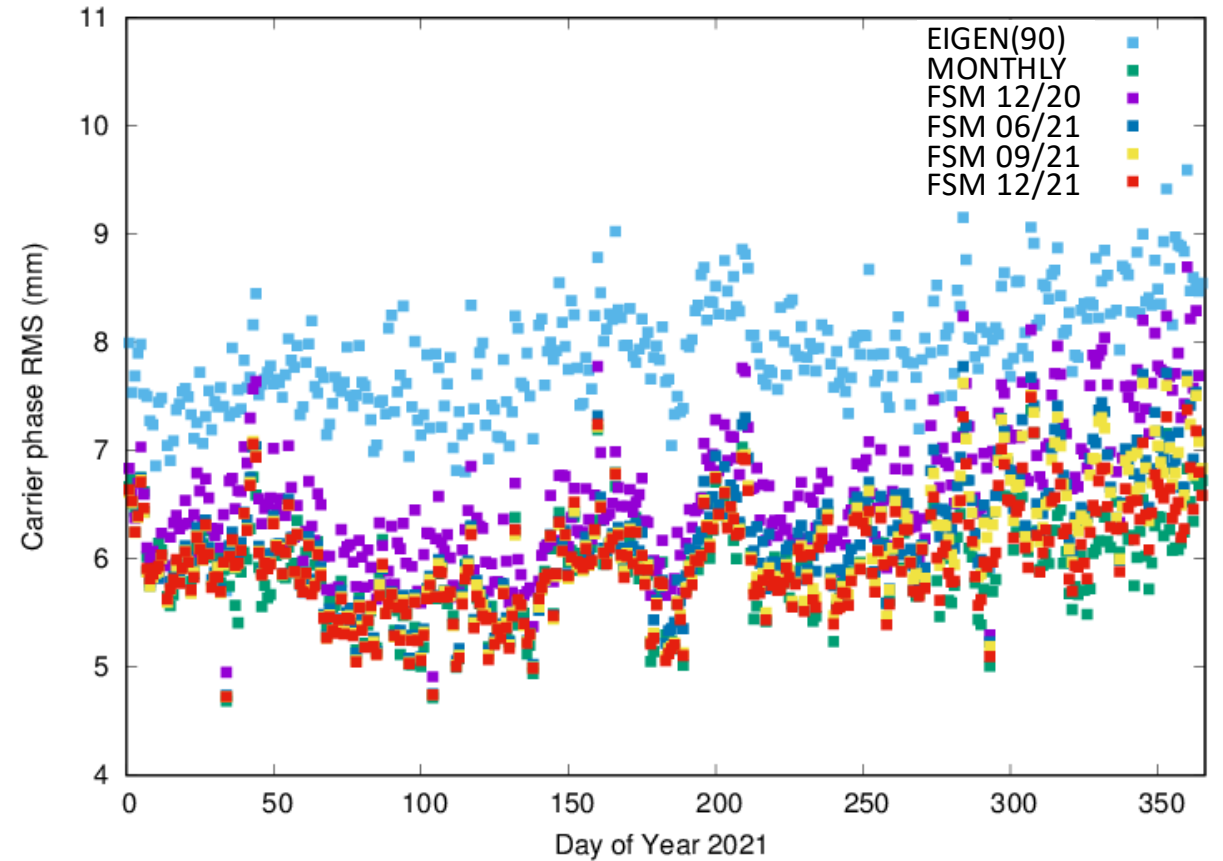
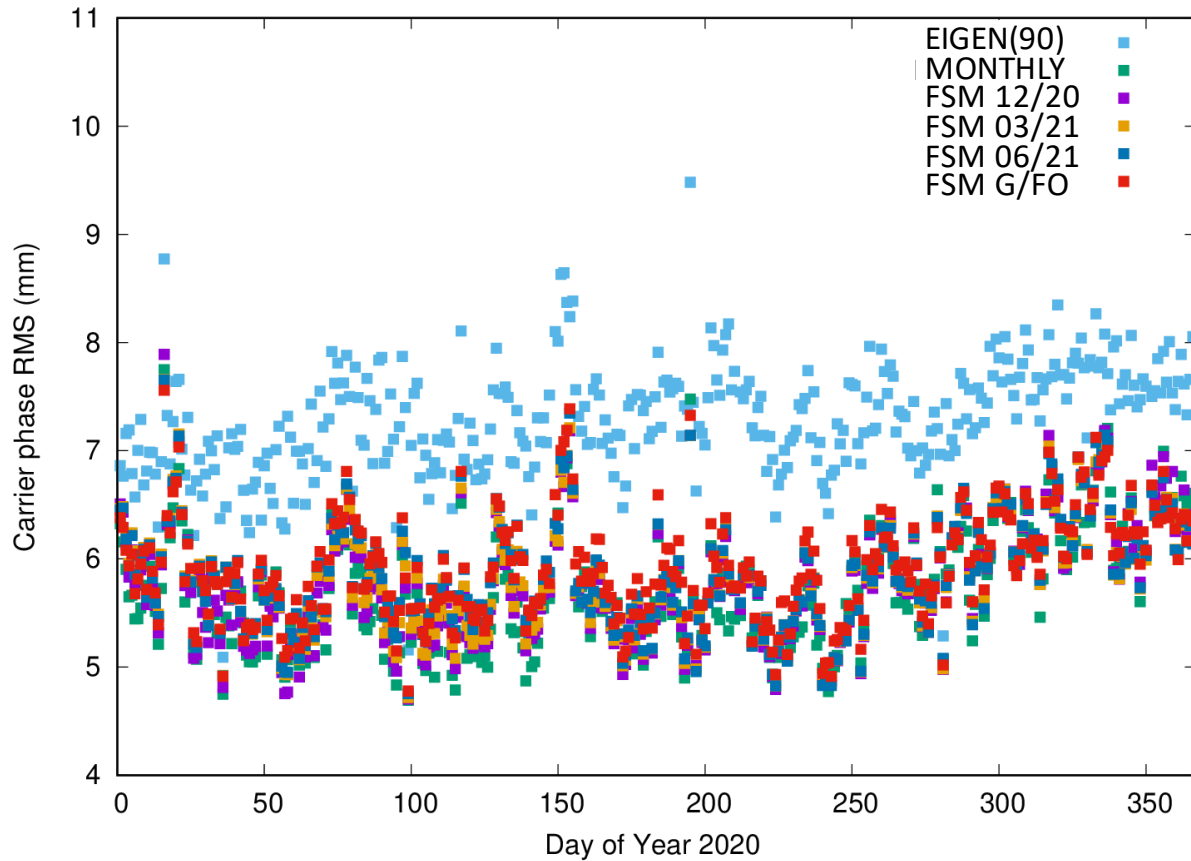
The time-series of monthly GRACE gravity field solutions was fitted in yearly batches for the EIGEN-GRGS-RL04 model.

While the fit in the GRACE period is very good, the extrapolation of the last of these batches leads to large errors in river basins with strong non-seasonal variations.

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# Application to Sentinel orbit POD

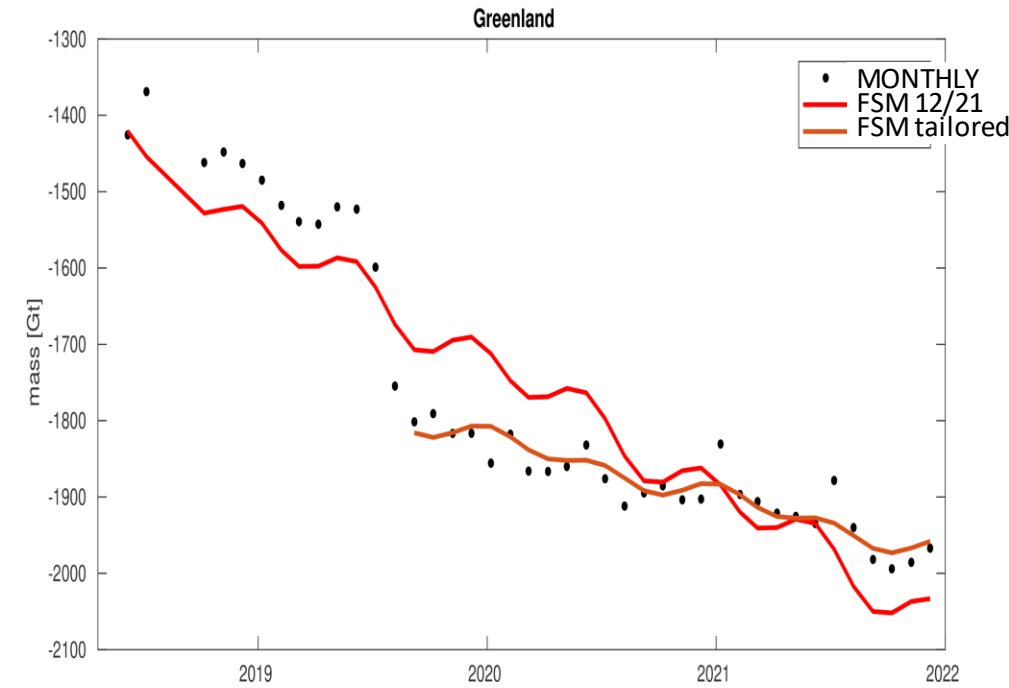
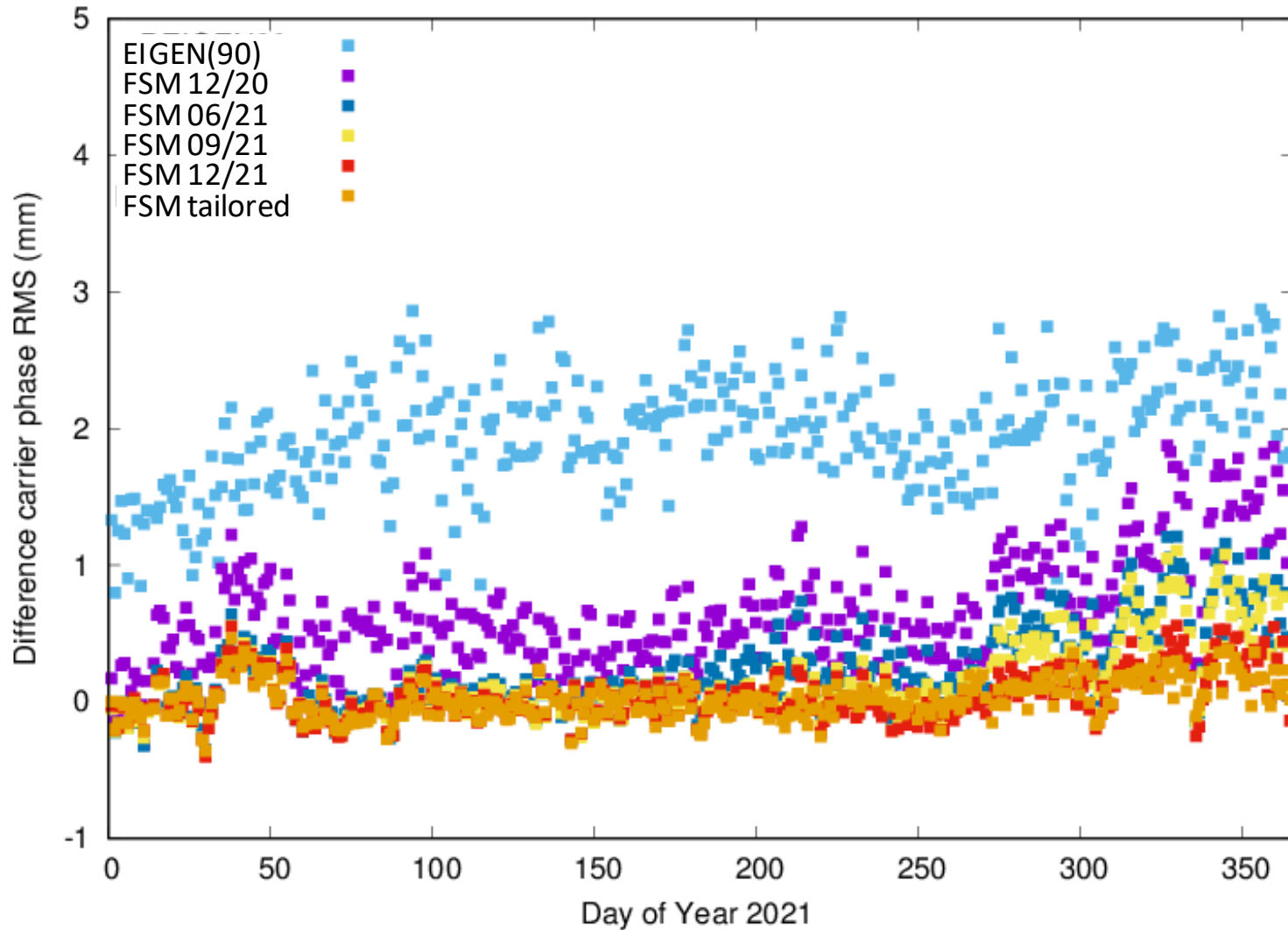
# Sentinel - 3B (altitude 811 km) orbit determination



The carrier phase RMS of dynamic Sentinel-3B satellite orbits (orbit altitude 811 km) based on monthly GRACE-FO gravity fields (green) or different fitted signal models reveals the benefit of up-to-date models. All models were truncated at max. degree/order 90.



# Impact of fit period on LEO-POD (Sentinel-3B, altitude 811 km)



Carrier phase residuals of Sentinel-3B orbits (811 km orbit altitude) confirm the sensitivity on the data period that entered the model.

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# Independent orbit validation

# SLR-validation Sentinel-3B

Data: Year 2020, Sentinel-3B, SLR validation, 12 stations (cm)

Gravity field model	Mean (cm)	RMS (cm)	Standard deviation (cm)
DEIGEN120	0.29	1.01	0.97
DEIGEN90	0.29	1.01	0.97
D90MONTHLY	0.28	0.91	0.87
<b>D90MODEL2012</b>	<b>0.28</b>	<b>0.92</b>	<b>0.88</b>
RDEIGEN120	0.31	0.91	0.85
RDEIGEN90	0.31	0.91	0.85
RD90MONTHLY	0.31	0.88	0.82

The limited max. degree does not negatively affect LEO POD (S3B)

LEO POD profits from monthly gravity fields

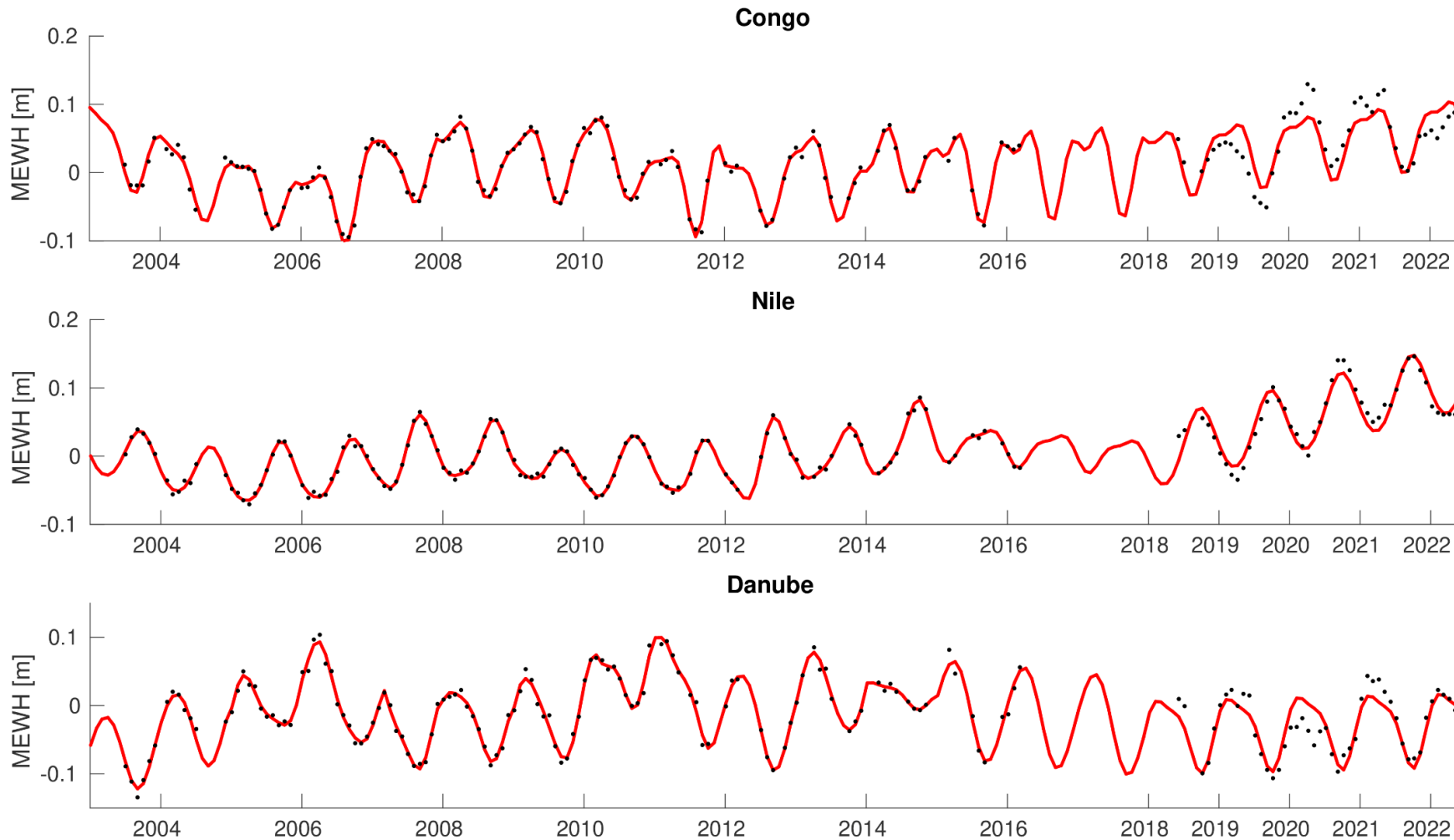
The fitted signal models perform close to the monthly gravity fields

Reduced dynamic LEO POD is less sensitive to model deficiencies.

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# Outlook

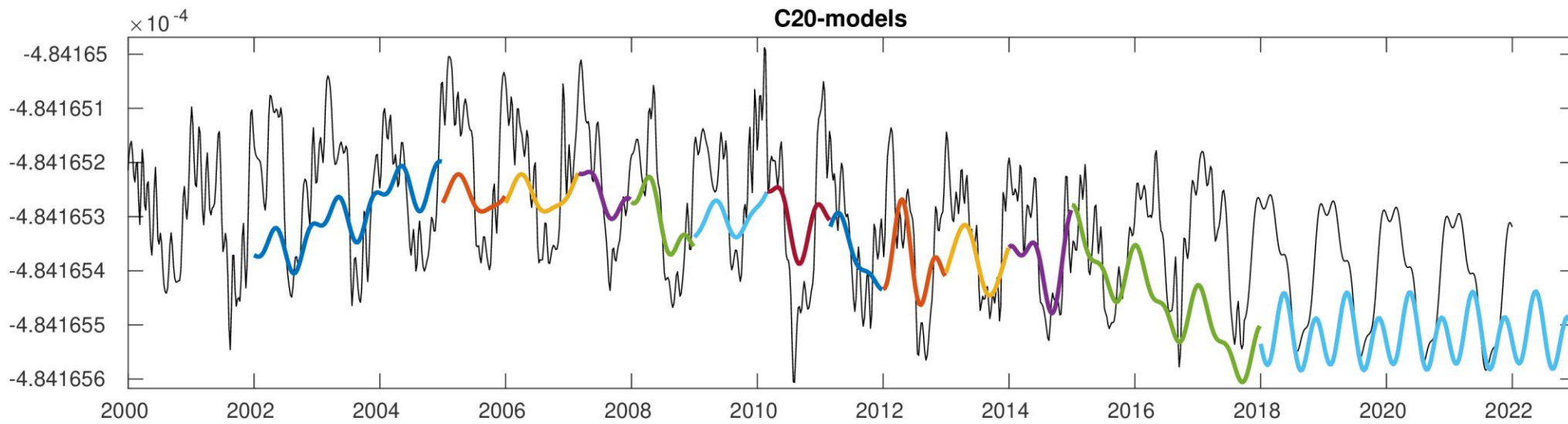
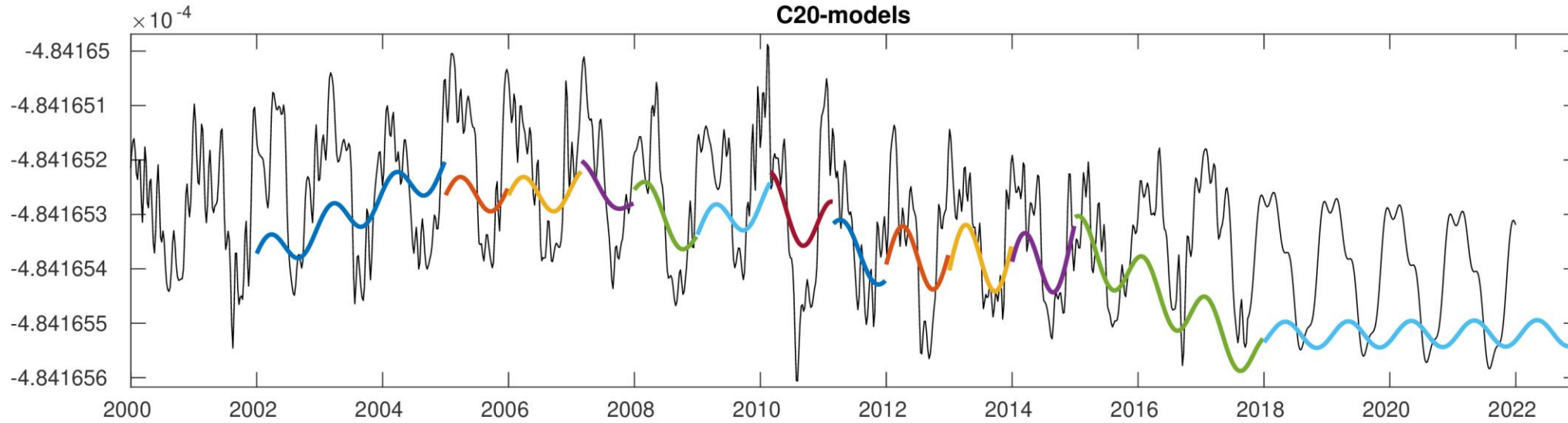
# Extension of COST-G FSM for REPRO purposes



Extension of the COST-G FSM to cover the whole GRACE/FO period:

- Fit of GRACE monthly models in yearly batches
- Continuity conditions between individual batches
- Fit of GRACE-FO monthly models in one batch to allow for prediction.

# Comparison of C20-Models



# LAGEOS 7d-solutions (obits/stations/ERPs/GCM)

No 1/rev. cross-track par.	X-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]	Y-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]
GGM05S (static)	66.3	261.1	86.5	245.8
ILRS (time-var.)	54.3	219.4	88.0	201.1
COST-G FSM (time-var.)	<b>51.0</b>	<b>215.6</b>	<b>80.6</b>	<b>196.7</b>

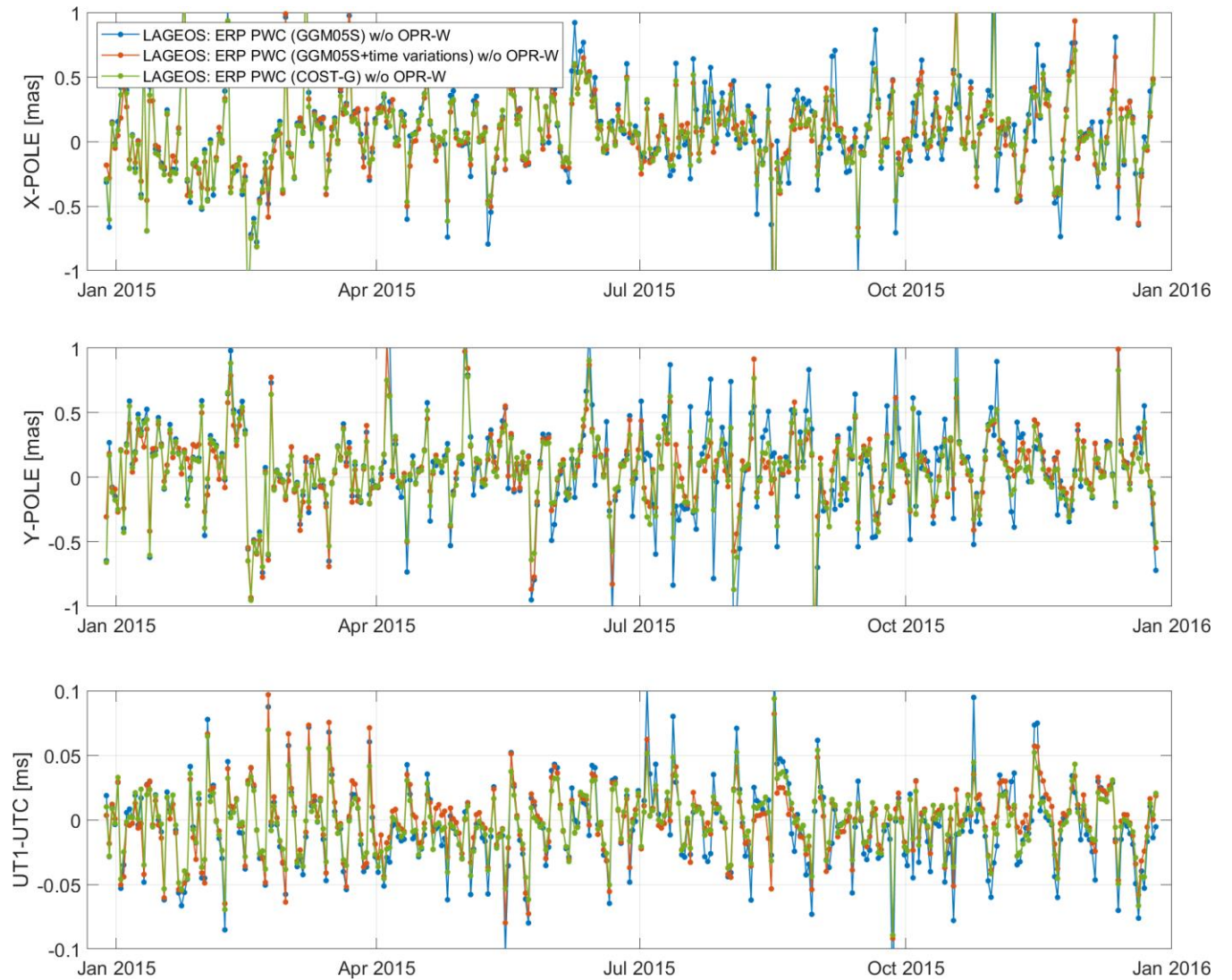
+ periodic cross-track	X-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]	Y-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]
GGM05S (static)	91.4	148.1	68.4	119.8
ILRS (time-var.)	73.7	142.3	75.9	126.2
COST-G FSM (time-var.)	<b>68.8</b>	<b>132.8</b>	<b>66.0</b>	<b>117.8</b>

+ C20	X-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]	Y-pole: bias [ $\mu\text{as}$ ]	RMS [ $\mu\text{as}$ ]
GGM05S (static)	68.8	175.9	72.2	<b>156.1</b>
ILRS (time-var.)				
COST-G FSM (time-var.)	<b>49.3</b>	<b>164.5</b>	<b>65.5</b>	157.2



# LAGEOS 7d-solutions (obits/stations/ERPs/GCM)

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