

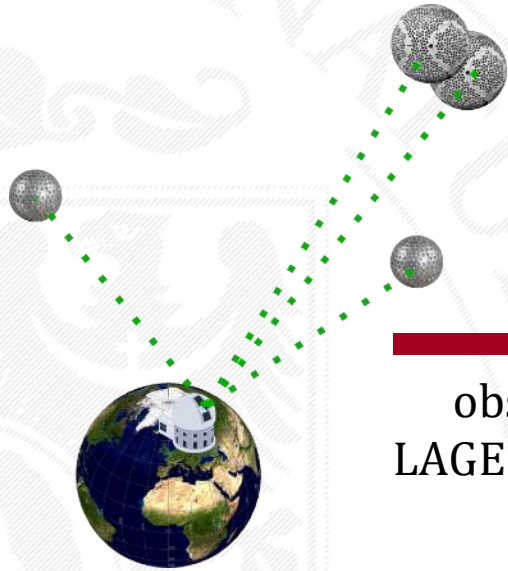


A SIMULATION STUDY FOR FUTURE GEODETIC SATELLITE CONSTELLATIONS



Joanna Najder, Krzysztof Sońnica,
Dariusz Strugarek, Radosław Zajdel

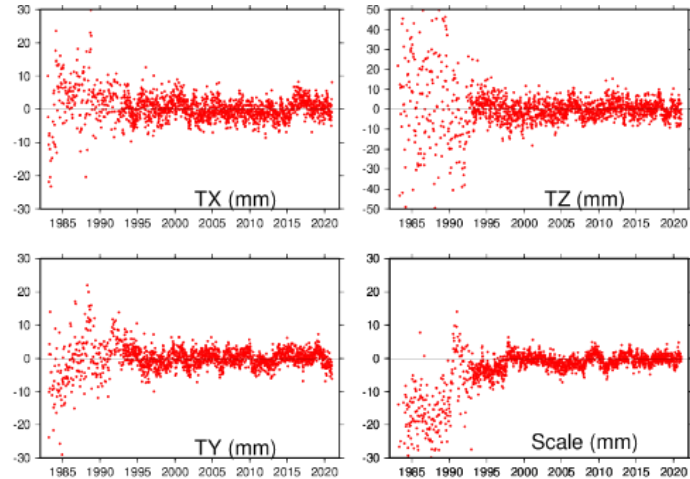
SATELLITE LASER RANGING



Geocenter coordinates

Origin and scale - ITRF

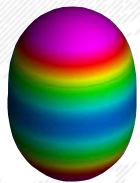
observations to the
LAGEOS-1/-2, Etalon 1/2



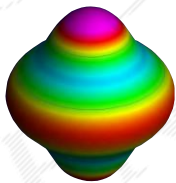
Earth's rotation parameters

SLR station coordinates

Low-degree harmonics of the Earth's
gravity potential

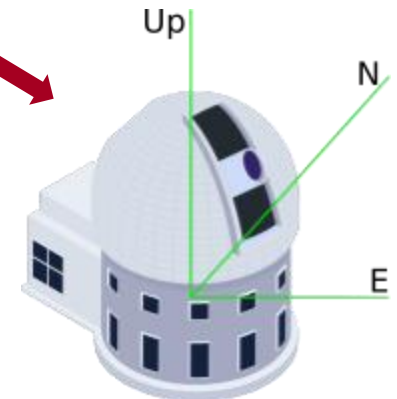
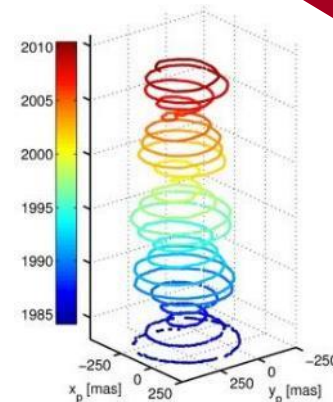
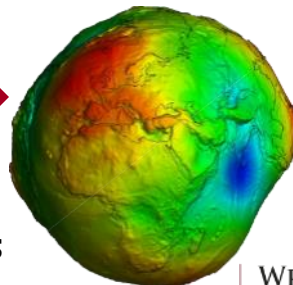


C_{20}



C_{30}

coefficients C_{20} and
 C_{30} are replaced by
SLR-based estimates

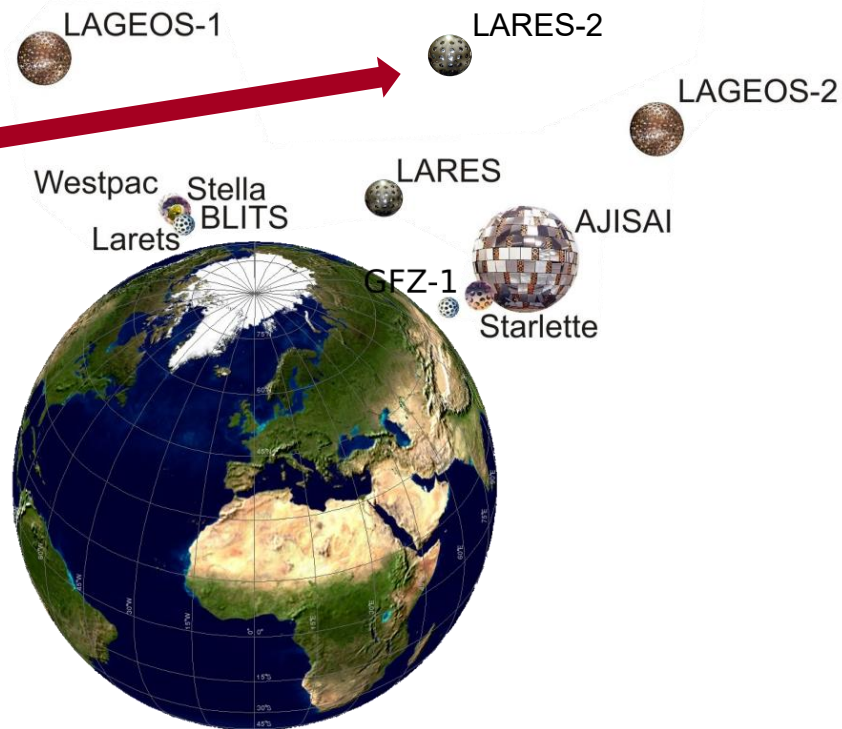


MOTIVATION



New geodetic satellite – LARES 2 was launched on 13 July 2022.

The main task of the LARES 2 is to study general relativity measurements, particularly the Lense-Thirring effect.



The increasing number of observation targets for SLR stations, e. g., space debris, or next navigation satellites.

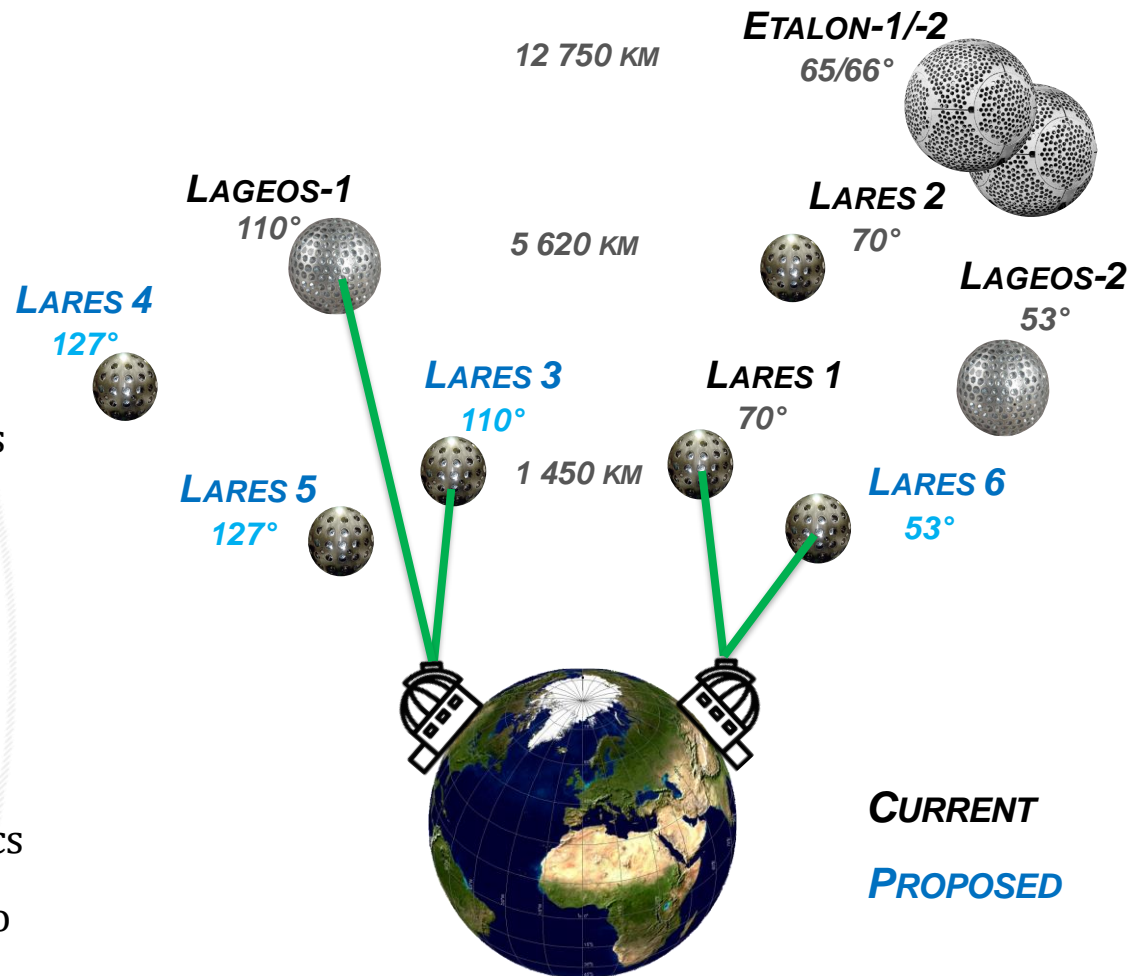
MOTIVATION

Investigate the impact of adding observations of the proposed satellites on the determination of geodetic parameters:

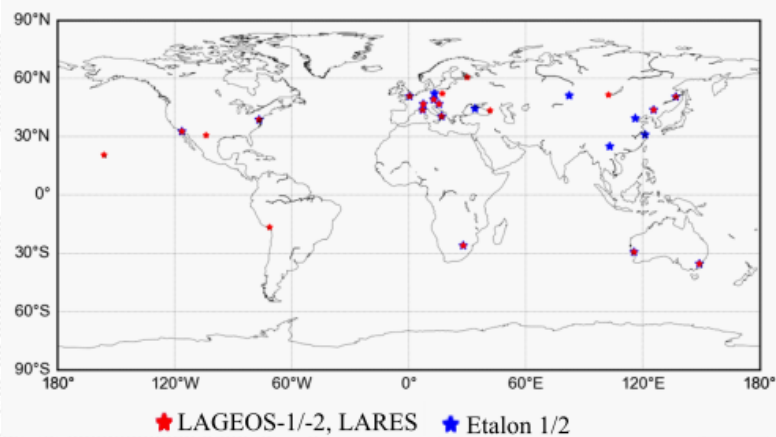
- ERPs,
- Geocenter (GCC),
- SLR station coordinates,
- The low-degree spherical harmonics of the Earth's gravity field up to d/o

6/6 GOALS:

- What will be the influence on global geodetic parameters when taking the observations of LARES 2 into account?
- What shall be the orbit parameters for future satellites that will bring the greatest improvement in determining geodetic parameters?



DATA PROCESSING



set of six Keplerian elements



1

orbit simulation



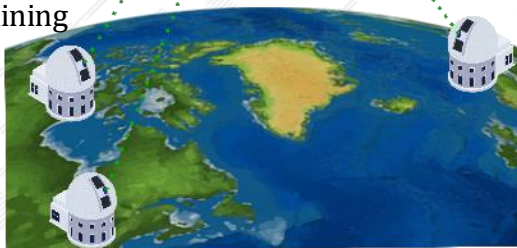
2

observation simulation



3

NEQ stacking
parameters determining



4

- LAGEOS-1/-2, Etalon-1/-2, LARES 1/2/3/4/5/6
- 20 of the best-performing SLR stations
- Year of simulated orbits and SLR observations (2013)
- 7-day solutions
- The number of simulated observations corresponds with the number of real observations

LAGEOS-1/-2 ~ 2600

Etalon 1/2 ~ 400

LARES ~ 1600

- Different observation noises for satellites:

LAGEOS-1/-2, LARES 2/4: 6 mm

LARES 1/3/5/6 : 9 mm

Etalon 1/2: 15 mm

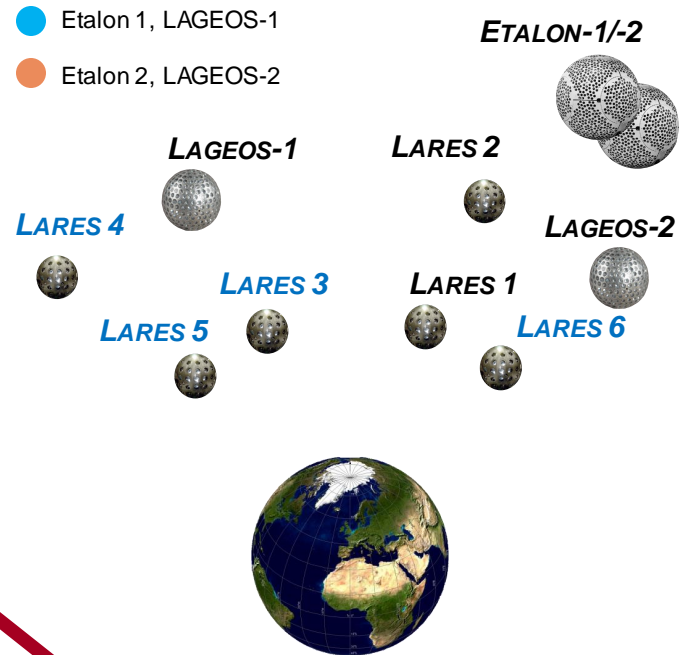
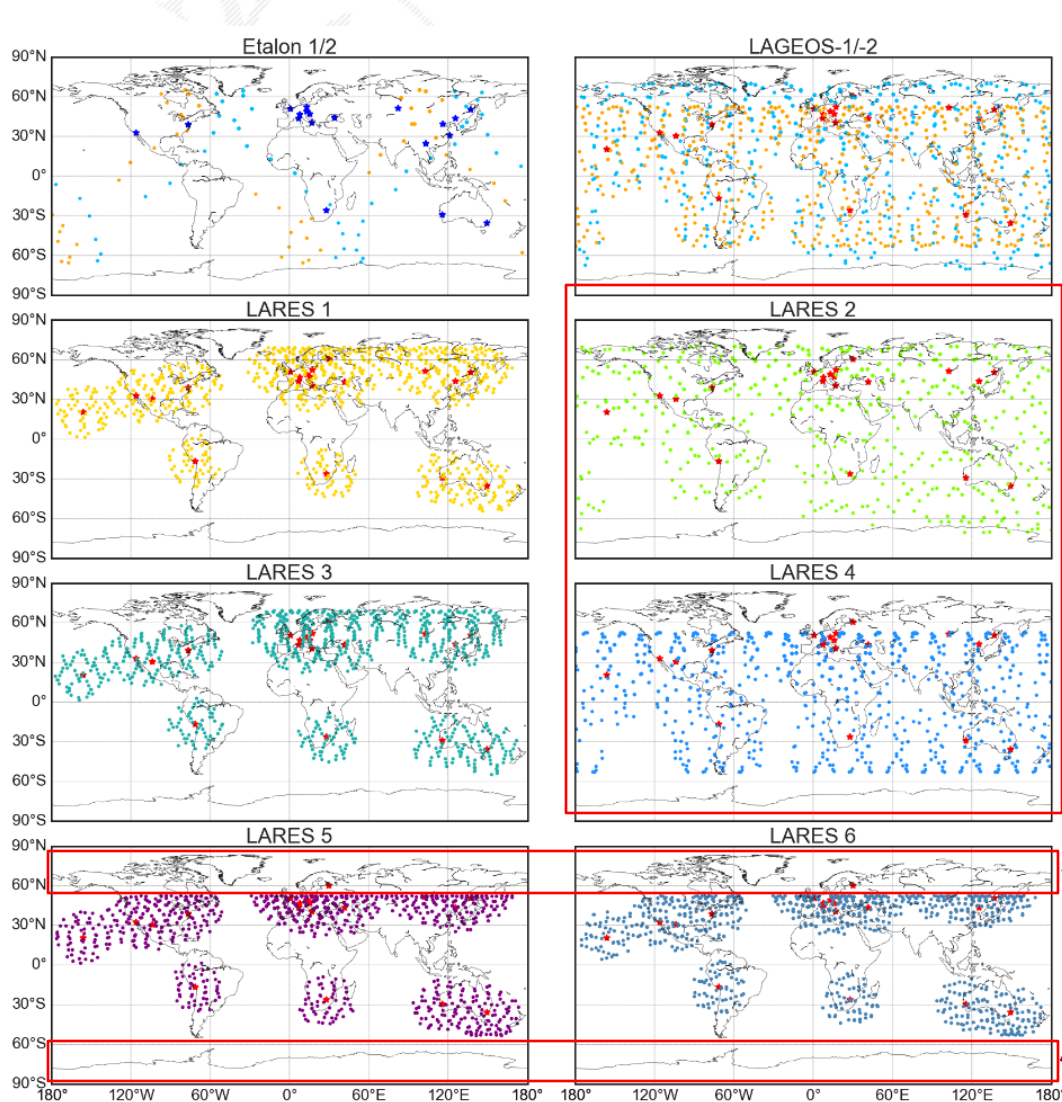
- Relative weighting on individual satellites in the combined solutions:

LAGEOS-1/-2, LARES 2/4: $\sigma^2 = 1.0$

LARES 1/3/5/6 : $\sigma^2 = 0.44$

Etalon 1/2: $\sigma^2 = 0.25$

DISTRIBUTION OF SIMULATED OBSERVATIONS

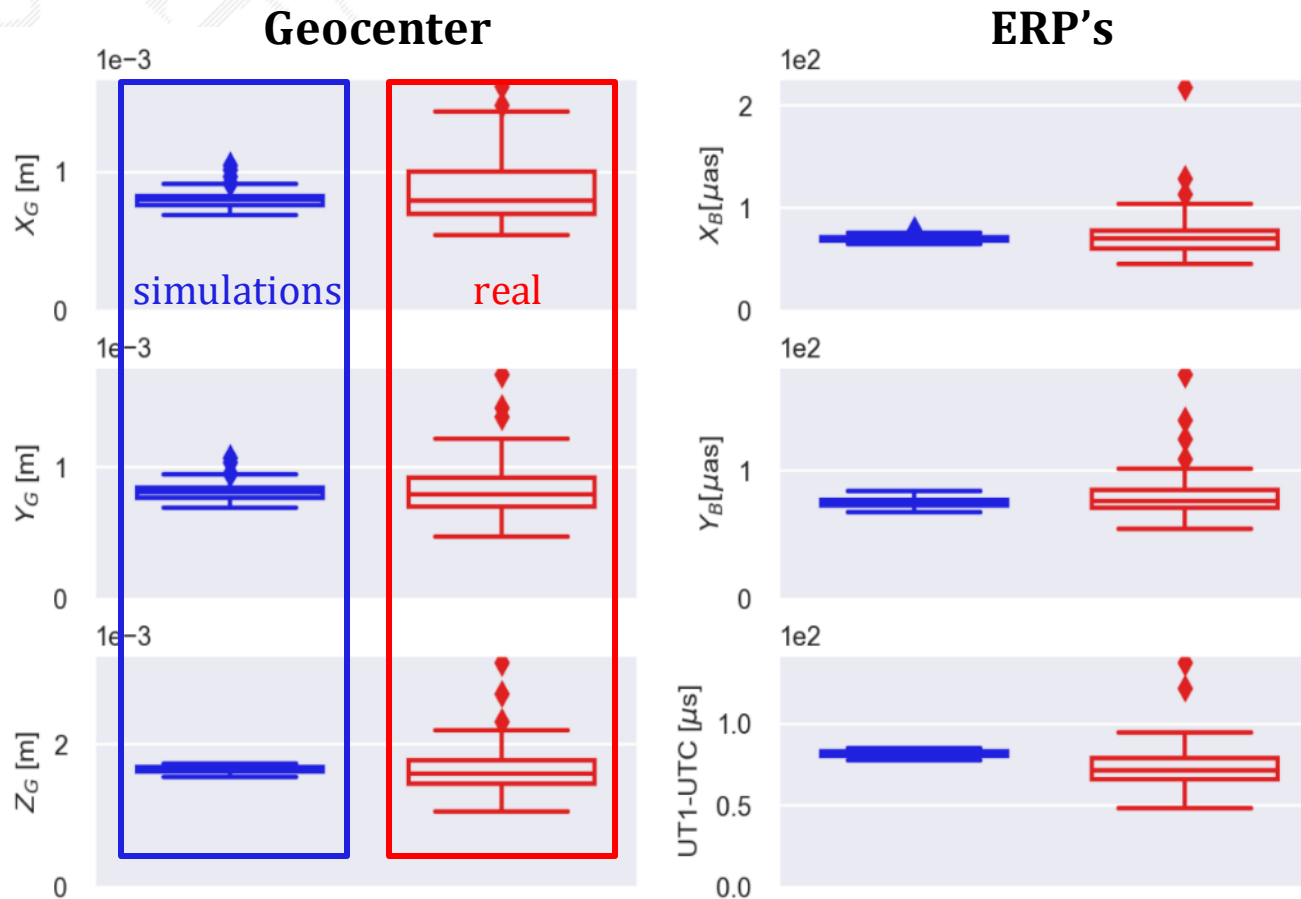


For satellites on MEO the distribution of observations is more dispersed

For satellites on LEO – LARES 5 and LARES 6 no normal points are collected for heights over/below 50° latitude

Presented distribution of simulated observations corresponds the distribution of real observations

COMPARING THE SOLUTIONS BASED ON REAL OBSERVATIONS TO SIMULATION RESULTS



We also compare the results achieved for simulated data with the solution obtained for the real observations of LAGEOS-1/-2 satellites. These solutions agree well in terms of the consistency of the formal error values of the obtained parameters of the ERP and the geocenter.

RESULTS

STATION COORDINATES

The current constellation of geodetic satellites based on LAGEOS-1/-2 and LARES 1/2 satellites in weekly solutions allows to determine station coordinates with formal errors

Solution	below 2° [mm]	N [mm]	Up [mm]
LAGEOS-1/-2 + LARES 1	2.2	2.3	2.0
LAGEOS-1/-2 + LARES 1/2	1.9	1.9	1.7
LAGEOS-1/-2 + LARES 1/2/4	1.7	1.8	1.5



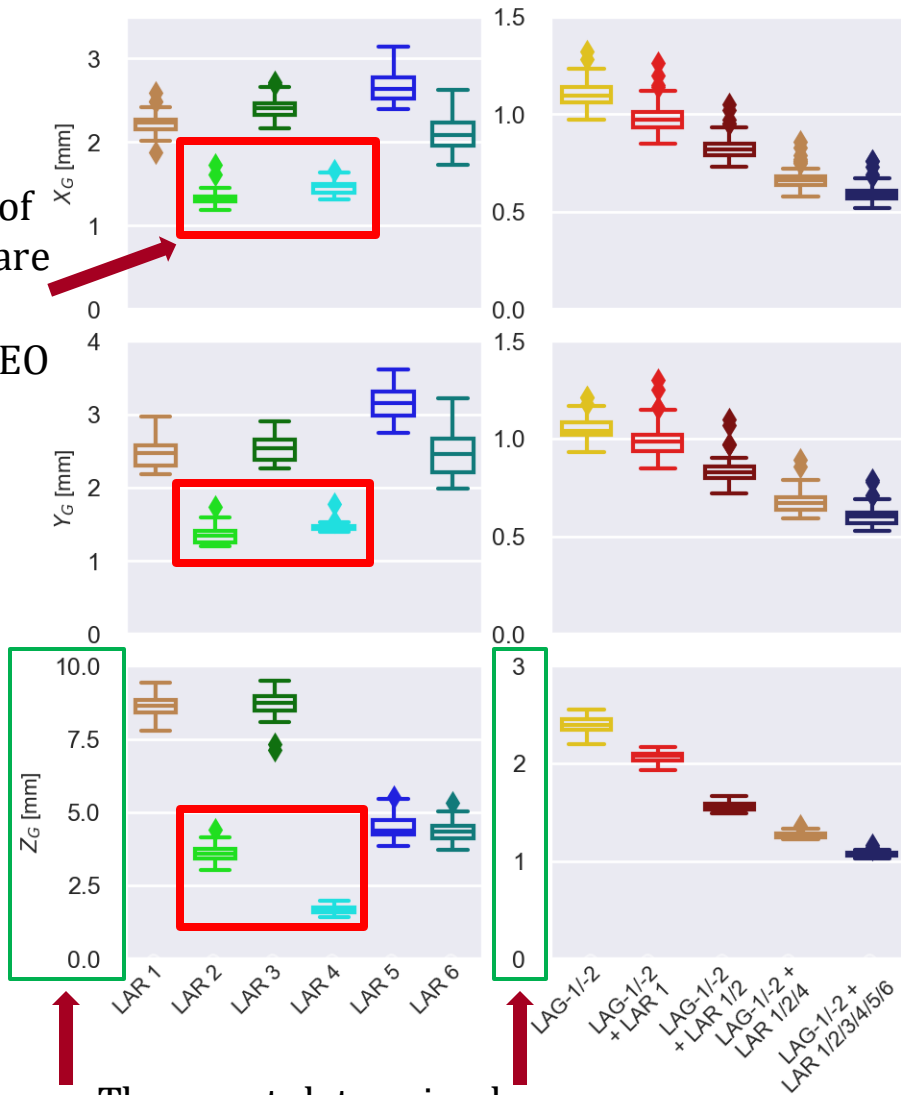
By adding observations of LARES 2 – reducing formal errors for stations, especially located at higher latitudes

By adding observations of LARES 4 – reducing formal errors for stations, especially located at lower latitudes

RESULTS

GEOCENTER COORDINATES

The medians of formal errors are smaller for satellites on MEO



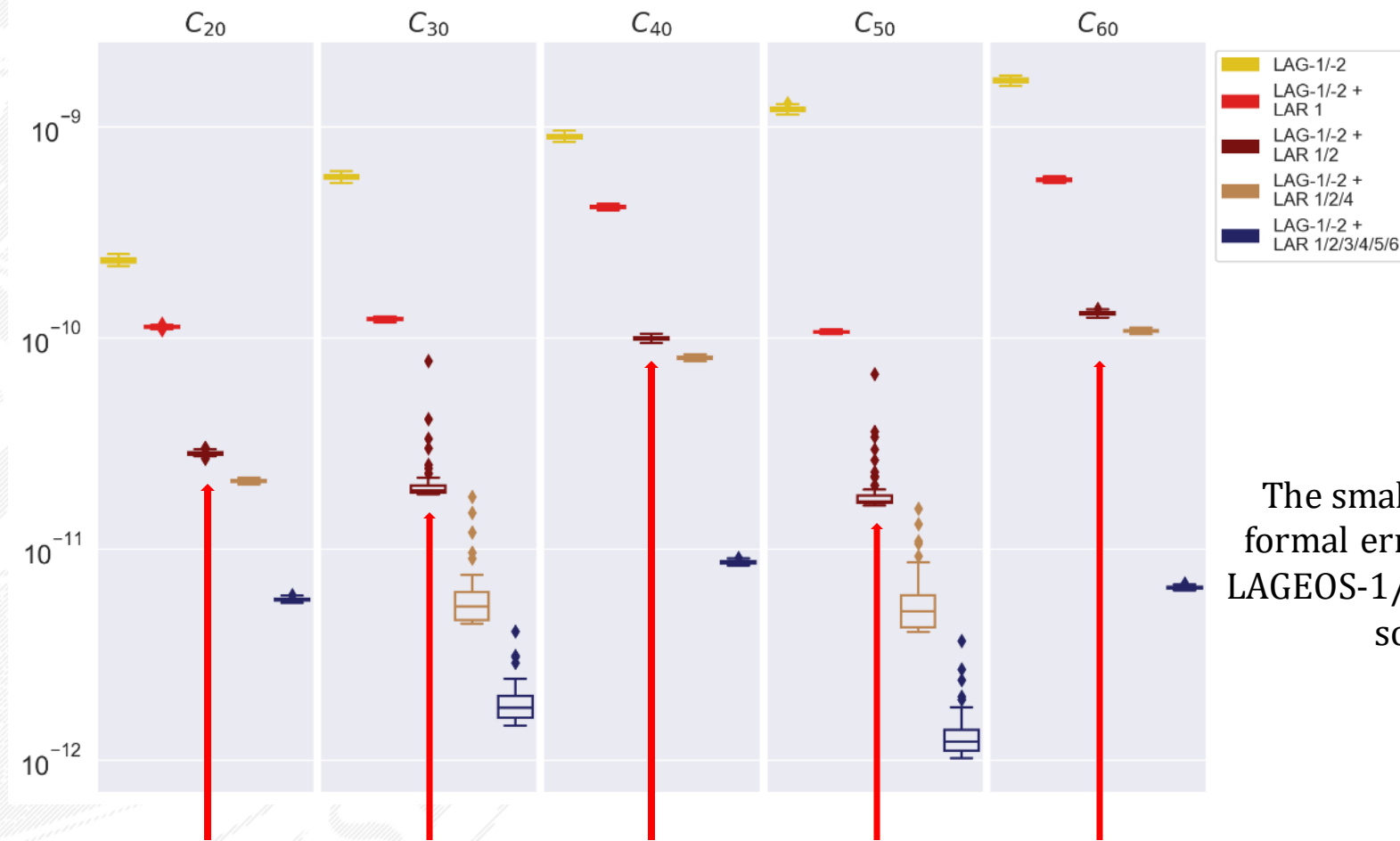
The worst determined component is Z geocenter

Solution LAGEOS-1/-2 + LARES 1/2 decreases formal errors by 20, 20, and 33% for X, Y, and Z, respectively with reference to LAGEOS-1/-2 + LARES 1 solution

Satellites	X [mm]	Y [mm]	Z [mm]
LAGEOS-1/-2	1.1	1.0	2.4
LAGEOS-1/-2 + LARES 1	1.0	1.0	2.1
LAGEOS-1/-2 + LARES 1/2	0.8	0.8	1.6
LAGEOS-1/-2 + LARES 1/2/4	0.7	0.7	1.3
LAGEOS-1/-2 + LARES 1-6	0.6	0.6	1.1

RESULTS

EARTH'S GRAVITY POTENTIAL – ZONAL HARMONICS

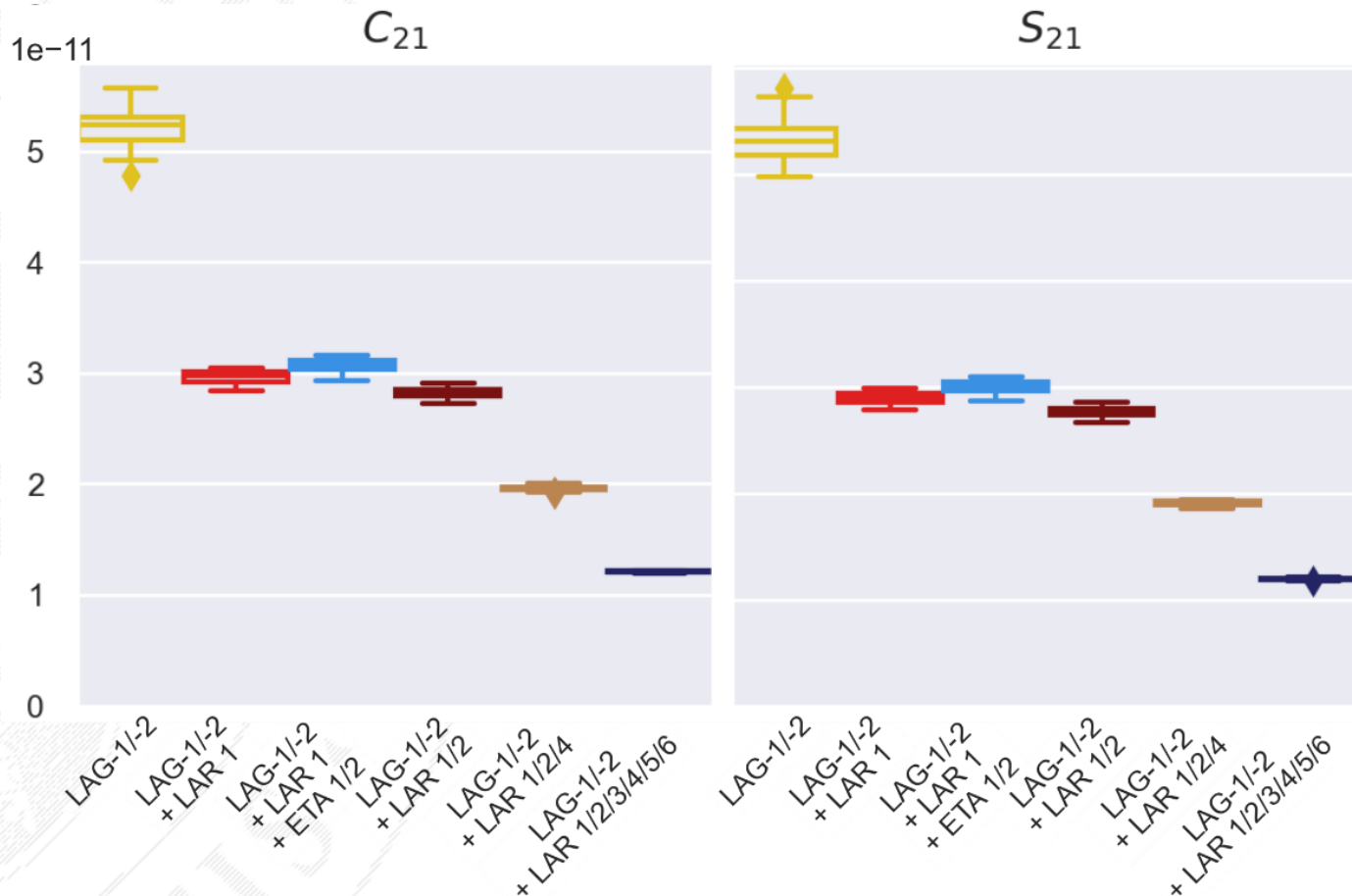


The smallest values of formal errors are for the LAGEOS-1/-2 + LARES 1-6 solution

Adding observations to LARES 2 to solutions LAGEOS-1/-2 + LARES 1 could decrease formal errors for zonal terms by one order of magnitude

RESULTS

EARTH'S GRAVITY POTENTIAL – C_{21} AND S_{21}



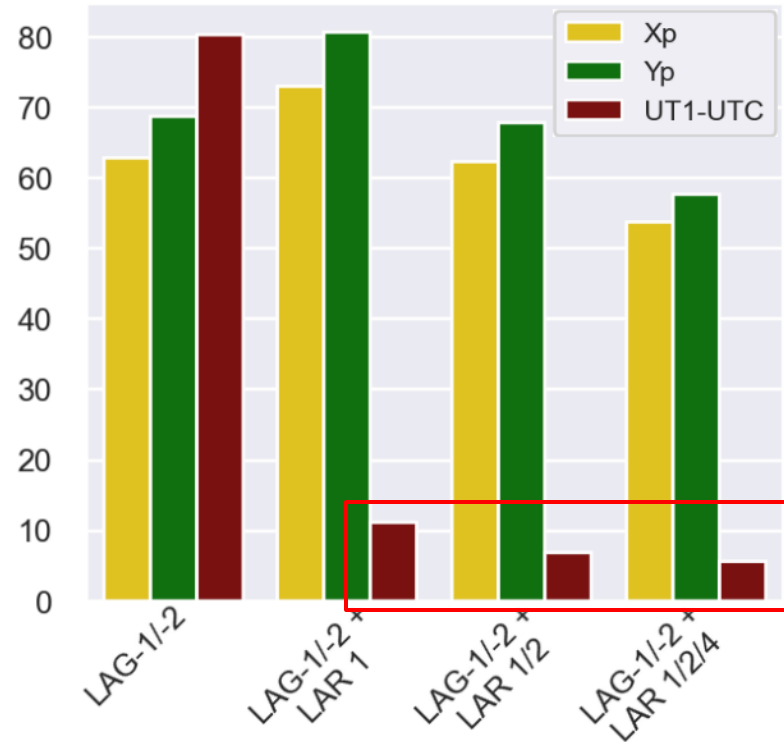
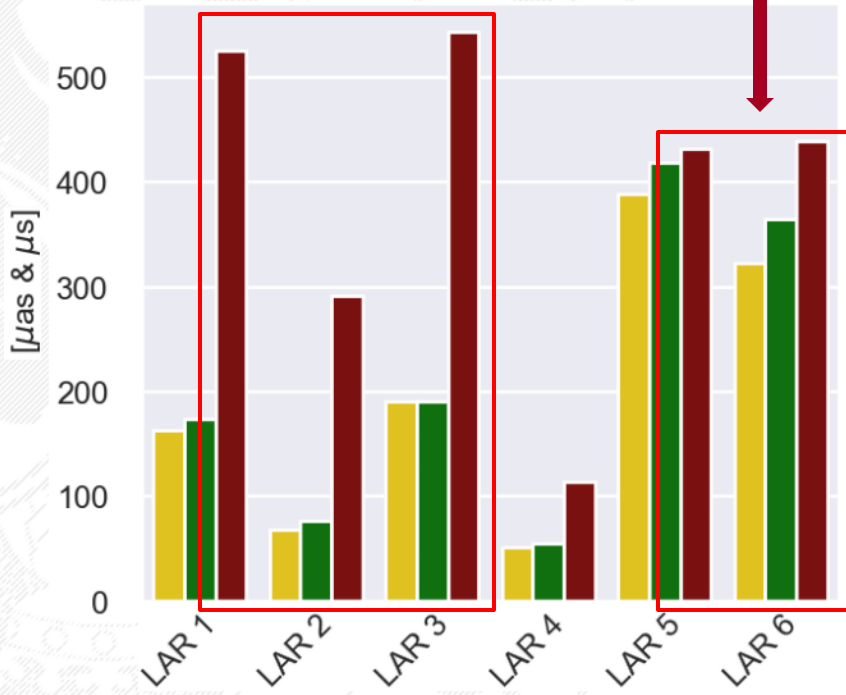
The observations of LARES 1 satellite could significantly improve the quality of determined C_{21} and S_{21} coefficients compared to observations of LARES 2 satellite.

RESULTS

EARTH'S ROTATION PARAMETERS

The satellites in almost polar orbits increase the formal errors for UT1-UTC

The satellites orbiting close to the equatorial plane increase the formal errors for the pole coordinates



	X _p [µs]	Y _p [µs]	UT1-UTC [µs]
LEO satellites	0.26	0.28	0.48
MEO satellites	0.06	0.07	0.20

Adding observations to LARES 1/2/4 satellites decreases the formal errors for UT1-UTC

LARES 2/4

CONCLUSION

ANSWER TO THE QUESTIONS:

- What will be the influence on global geodetic parameters when taking the observations of LARES 2 into account?

Adding observations will improve the quality of the parameters determined not only by a greater number of observations, but also by adding observations to satellites with different altitudes and orbit inclinations, causing the correlations between estimated parameters are reduced. The greatest reduction in formal errors should occur for the coordinates of the SLR stations, as well as for the geocenter coordinates - in particular for the Z component.

- What shall be the orbit parameters for future satellites that will bring the greatest improvement in determining geodetic parameters?

The biggest improvement would be for the LARES 4 satellite, which would supplement the current constellation – LARES 4 satellite will be the **retrograde satellite, orbiting symmetrical to the LAGEOS-2.**



WROCLAW UNIVERSITY
OF ENVIRONMENTAL
AND LIFE SCIENCES

THANK YOU FOR YOUR ATTENTION!



Joanna Najder, Krzysztof Sośnica,

Dariusz Strugarek, Radosław Zajdel

Institute of Geodesy and Geoinformatics